

DOON UNIVERSITY, DEHRADUN

Department of Mathematics, School of Physical Sciences Mid Semester Examination, Even Semester 2017-18

Class: Int.M.Sc.Mathematics

Course: Linear Programming

Time Allowed: 2 Hours

Semester: VI

Course Code: MAD-353

Max Marks: 30

Note: Attempt all Four questions in Section A. Each question carries 1.5 marks.

Attempt any Three questions in Section B. Each question carries 4 marks.

Attempt any **Two** questions in Section C. Each question carries **6** marks.

Section: A

(Very Short Answer Type Questions)

Attempt all Four questions.

 $[4 \times 1.5 = 6 \text{ Marks}]$

- 1. Describe the following terms (i) Basic feasible solution (ii) Convex hull (iii) Hyperplane.
- 2. Examine the convexity of the set $S = \{(x_1, x_2) : x_1 \le 2, x_2 \le 3, x_1 \ge 0, x_2 \ge 0\}.$
- 3. Write the dual of the linear programming problem(LPP):

Maximize $Z = 2x_1 + 3x_2 + 4x_3$

Subject to: $2x_1 + 2x_2 + 3x_3 \le 4$; $3x_1 + 4x_2 + 5x_3 \ge 5$; $x_1 + x_2 + x_3 = 7$, $x_1, x_2, x_3 \ge 0$.

4. Prove that dual of the dual is primal.

Section B

(Short Answer Type Questions)

Attempt any Three questions.

 $[3\times4=12 \text{ Marks}]$

- 5. Prove that a set S is convex iff every convex linear combination of points in S belongs to S.
- 6. Prove that in a LPP if the optimum of f(X) occurs at an interior point X_0 of S_F , then f(X) is constant throughout S_F (set of feasible solutions).
- 7. Use Graphical method for solving the following LPP:

Maximize $Z = 5x_1 + 3x_2$

Subject to: $4x_1 + 5x_2 \le 10$; $5x_1 + 2x_2 \le 10$; $3x_1 + 8x_2 \le 12$; $x_1, x_2 \ge 0$.

8. Use Simplex method to solving the following LPP:

Maximize $Z = 2x_1 + 5x_2 + 7x_3$

Subject to: $3x_1 + 2x_2 + 4x_3 \le 100$; $x_1 + 4x_2 + 2x_3 \le 100$; $x_1 + x_2 + 3x_3 \le 100$; $x_1, x_2, x_3 \ge 0$.

Section C

(Long Answer Type Questions)

Attempt any Two questions.

 $[2\times6=12 \text{ Marks}]$

- 9. Prove that a vertex of $S_F \iff$ a basic feasible solution (B.F.S.).
- 10. Solve the following LPP using Two-Phase method:

 $Minimize Z = x_1 + x_2 + x_3$

Subject to: $x_1 - 3x_2 + 4x_3 = 5$; $x_1 - 2x_2 \le 3$; $2x_2 + x_3 \ge 4$; $x_1, x_2 \ge 0$ and x_3 is unrestricted.

11. Solve the following LPP using Big-M method:

Maximize $Z = x_1 + 2x_2 + 3x_3 - x_4$

Subject to: $x_1 + 2x_2 + 3x - 3 = 15$; $2x_1 + x_2 + 5x_3 = 20$; $x_1 + 2x_2 + x_3 + x_4 = 10$; $x_1, x_2, x_3, x_4 \ge 0$.